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## **Integrating Factors in Market Indexes and Active Portfolios**

DIMITRIS MELAS, ZOLTÁN NAGY, NAVNEET KUMAR, AND PETER ZANGARI







#### **DIMITRIS MELAS,** Managing Director and Global Head of Core Equity Research

Dimitris Melas is Managing Director and Global Head of Core Equity Research at MSCI, where he is responsible for equity research and strategic product development across both equity indexes and equity analytics. Dimitris leads a global team of research specialists. Prior to joining MSCI in 2006, Dimitris worked at HSBC Asset Management as Head of Research and Head of Quantitative Strategies. He is a Chartered Financial Analyst and holds an MSc in Electrical Engineering, an MBA in Finance, and a PhD in Applied Probability from the London School of Economics. He has published research papers in peer-reviewed journals and serves as Editorial Board Member of *The Journal of Portfolio Management*.

#### ZOLTÁN NAGY, Executive Director, Equity Core Research

Zoltán Nagy is a member of the Equity Core Research team. In this role, he focuses on questions related to the integration of factors and ESG considerations into the equity portfolio management process. Zoltan joined MSCI in 2008, and first worked on the development of new index methodologies and on other index-related research. Prior to entering finance, Zoltan was a post-doctoral researcher at the University of Algarve, Faro, Portugal, where his area of research was Quantum Integrable Systems. Zoltan holds a PhD degree in Theoretical Physics from the University of Cergy-Pontoise, France, and an engineering degree from the Ecole Polytechnique, France. He is also a CFA<sup>®</sup> charterholder.



#### NAVNEET KUMAR, Vice President, MSCI Core Equity Research Team

Navneet Kumar is a Vice President in the MSCI Core Equity Research Team, which conducts proprietary research and strategic product development to address clients' investment problems. Previously, he worked as quantitative analyst with HSBC and ARP Research. Navneet is a Chartered Financial Analyst and holds MSc in Mathematics from the Indian Institute of Technology (IIT) Bombay.



#### PETER ZANGARI, Global Head of Research and Product Development

Peter Zangari sets MSCI's research agenda and drives integration of research into MSCI's products and services to deliver innovative solutions to investment problems. He is a member of the Executive Committee.

Previously, Peter served as Head of Analytics at MSCI, responsible for its equity and multi-asset class risk and portfolio management products, and was Head of Equity Portfolio Management Analytics before that. Prior to joining MSCI, Peter held senior-level positions at Goldman Sachs, including as the Head of Risk and a member of the leadership team for Goldman Sachs Asset Management's Quantitative Investment Strategies business. Peter began his career at JP Morgan in the RiskMetrics and Firmwide Risk groups. Peter has a B.A. in economics from Fordham University and a Ph.D. in economics, with a specialization in applied econometrics and computational statistics, from Rutgers University.

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#### DIMITRIS MELAS

is a managing director at MSCI, Inc. in London, UK. **dimitris.melas@msci.com** 

#### Zoltán Nagy

is an executive director at MSCI, Inc. in Budapest, Hungary. zoltan.nagy@msci.com

#### NAVNEET KUMAR is a vice president at MSCI, Inc. in Mumbai, India. navneet.kumar@msci.com

PETER ZANGARI

is a managing director and global head of research and product development at MSCI, Inc. in New York, NY. **peter.zangari@msci.com** 

\*All articles are now categorized by topics and subtopics. **View at PM-Research.com.** 

**ABSTRACT:** *In this article, the authors review* factor performance in global equity markets using coherent data and methodology and apply a new template to evaluate their backtests for potential selection bias under multiple testing. They then propose a systematic process for integrating factor information into different investment strategies. The authors show that this process is consistent with the Black–Litterman framework and test it on a sample of market indexes and active equity portfolios. Integrating factors in indexes improved risk-adjusted performance while retaining high liquidity and capacity. Adding factors to active strategies enhanced information ratios while maintaining the portfolio characteristics and stock selection alpha of the original strategies. The authors' analysis may have important implications for different types of investors. Asset owners may be able to tilt reference indexes toward rewarded factors without sacrificing market coverage and diversification. Index managers can track factor-tilted indexes because they remain investable and replicable. Finally, active managers may be able to incorporate factor information into their strategies to harvest factor premiums while preserving their core investment process and the added value from fundamental security selection.

**TOPICS:** Factor-based models, portfolio management/multi-asset allocation, style investing\*

he theoretical foundations of factor investing can be traced back to pioneering academic research published several decades ago. Markowitz (1952) provided an analytically tractable definition of risk and established mean-variance optimization as a formal method for building portfolios by trading off risk and return. Sharpe (1964) introduced the capital asset pricing model, which elegantly captures the idea that the market is the most important common driver of portfolio performance. Ross (1976) extended the market model to include multiple factors that may exert common influences on asset prices and portfolio returns.

A substantial body of empirical research followed over the next four decades, aiming to establish the precise nature of the common factors affecting risk and return in different asset classes and markets. Many studies also proposed hypotheses explaining why some of these factors may be priced and therefore why assets and portfolios that emphasize these characteristics may earn positive excess returns. Potential explanations include systematic risk, behavioral bias, asymmetric information, and institutional constraints. In equities, eight factor groups have been documented through empirical research and have been used extensively in portfolio risk models and in active investment strategies:

value, size, momentum, volatility, quality, yield, growth, and liquidity.

Value and size were established early on as important common influences and potential sources of excess return (e.g., Basu 1977; Banz 1981; Brown, Kleidon, and Marsh 1983; and Fama and French 1993). Jegadeesh and Titman (1993) documented the existence of crosssectional momentum in US equities, and Carhart (1997) added momentum to the Fama and French three-factor model. Black (1972), Haugen and Baker (1991), and Frazzini and Pedersen (2014) documented the low-volatility effect and established volatility as an important equity factor and potential source of excess return.

Sloan (1996) showed that accounting accruals are negatively correlated with future stock returns, and Novy-Marx (2013) found that high-profitability companies earn higher returns despite having higher valuations. Profitability and earnings quality are often viewed as different dimensions of the quality factor. Other metrics used to quantify quality include financial leverage, earnings variability, and asset growth (investment quality). Several studies found a link between dividend yield and subsequent stock performance, including those by Blume (1980), Fama and French (1988), and Arnott and Asness (2003). Growth is a fundamental input into all valuation models and has been investigated in a number of empirical studies (e.g., Ofer 1975, Bauman and Dowen 1988, and Fama and French 2006). Finally, several studies have documented the link between liquidity and the cross section of returns, including those by Amihud and Mendelson (1989), Amihud (2002), and Pastor and Stambaugh (2003).

Despite the large number of studies examining factors, one challenge in evaluating the results is the lack of consistency in terms of data sources, definition of variables, portfolio construction methodology, geographical focus, and so on. Exhibit 1 shows historical performance statistics for the eight equity factors documented in the literature, using point-in-time data and a consistent methodology covering global equity markets over the period of December 31, 1994 to February 28, 2018. We examine different variables that are commonly used to quantify equity factors. The precise definitions of the variables we study can be found in Morozov et al. (2015). In addition, we estimate historical factor performance in three different and increasingly sophisticated settings that account for and help us understand the influence of all important performance drivers, including countries, industries, and other factors.

In the first setting, we formed equally weighted quintile portfolios sorted on a particular factor and examined the performance of a monthly rebalanced strategy that goes long the top quintile and short the bottom quintile. This simple strategy reflects the returns associated with a specific factor but also includes other influences, such as countries, industries, and other style factors. In the second setting, we run univariate cross-sectional regressions of stock returns against stock exposures to a particular factor. The regressions include indicator variables for countries and industries. Effectively, through this process we estimated factor returns net of country and industry influences. Finally, in the third setting, we ran multivariate cross-sectional regressions of stock returns against countries, industries, and all style factors. This process isolates returns associated with a particular factor, net of country, industry, and other factor effects.

The value factors we examined (book to price, earnings yield, long-term reversal) generated positive information ratios (IRs) across all three settings over the period we studied. In fact, IRs improved when we accounted for other influences, suggesting that value strategies have historically performed better when hedging other factors. On the other hand, size factors performed reasonably well in the simple long-short quintile setting; however, performance deteriorated when we accounted for other factors. Our analysis confirms the strong historical performance of momentum reported in other empirical studies. IRs remained high across all methods, suggesting that momentum strategies have worked well historically irrespective of hedging policy on other factors. The analysis of volatility factors shows that betting against beta has only produced small gains historically in simple settings, whereas low residual volatility performance has been consistently positive across different approaches.

Four of the five quality factors we examined (profitability, earnings quality, investment quality, and low earnings variability) had positive excess returns historically across all three-factor return estimation methods, whereas low leverage only had positive excess return in a multivariate setting. The yield factor had positive excess return across all methods. Growth only produced a positive IR in a multivariate regression, suggesting that growth strategies historically have performed better

#### **E** X H I B I T **1** Historical Performance of Global Equity Factors

		Equal-V	Veighted Portfolio	Quintile	;	I	.ong–Sh Quintil	ort es		Univar Regress	iate sion	N I	Iultivar Regress	riate ion
Factors	Q1	Q2	Q3	Q4	Q5	Ret.	Vol.	Sharpe	Ret.	Vol.	Sharpe	Ret.	Vol.	Sharpe
Value														
Book to Price	-2.09	-1.54	-0.67	0.38	3.93	6.01	13.1	0.46	1.70	3.55	0.48	1.84	1.58	1.16*
Earnings Yield	-3.72	-2.33	-0.46	1.45	5.06	8.78	13.3	0.66*	3.55	3.27	1.08*	2.37	2.04	1.16*
Long-Term Reversal	-3.96	-1.50	0.11	1.13	4.22	8.18	13.2	0.62*	1.70	2.21	0.77*	1.31	1.47	0.89*
Size														
Size	1.22	2.26	-0.48	-1.64	-1.38	-2.60	12.2	-0.21	-0.15	2.66	-0.05	-0.06	2.46	-0.02
Mid Cap	0.90	0.66	0.72	-0.52	-1.77	-2.67	10.5	-0.25	0.68	2.06	0.33	0.15	1.39	0.11
Momentum														
Momentum	-7.05	-3.56	0.42	3.73	6.49	13.54	21.4	0.63*	3.21	5.73	0.56	3.94	4.24	0.93*
Volatility														
Beta	0.41	0.15	-0.02	-0.46	-0.07	-0.47	26.6	-0.02	-1.04	6.88	-0.15	0.09	5.24	0.02
Residual Volatility	1.96	0.71	-0.51	-1.86	-0.29	-2.24	19.4	-0.12	-1.79	3.82	-0.47	-2.18	3.14	-0.69*
Quality														
Profitability	-1.62	-0.65	-0.35	0.38	2.23	3.85	7.09	0.54	1.72	2.26	0.76*	1.10	1.16	0.95*
Earnings Quality	-1.00	-1.45	-0.58	0.71	2.33	3.33	5.65	0.59*	1.33	1.46	0.91*	1.21	0.78	1.55*
Investment Quality	-3.68	-0.65	0.05	0.79	3.50	7.18	10.7	0.67*	2.21	2.09	1.06*	1.15	0.81	1.41*
Leverage	-0.70	0.55	-1.24	0.47	0.93	1.62	8.25	0.20	0.22	1.88	0.12	-0.11	1.11	-0.10
Earnings Variability	1.23	1.22	0.80	-0.34	-2.90	-4.13	12.8	-0.32	-1.30	3.58	-0.36	-0.33	1.26	-0.26
Yield														
Dividend Yield	-0.75	-0.70	-2.23	-0.06	3.72	4.48	13.1	0.34	2.20	2.63	0.83*	1.00	1.23	0.82*
Growth														
Growth	0.35	0.41	-0.62	0.36	-0.50	-0.85	11.4	-0.07	-0.12	2.48	-0.05	0.91	1.24	0.74*
Liquidity														
Liquidity	-0.22	0.52	0.98	0.76	-2.04	-1.83	16.4	-0.11	-0.79	3.35	-0.23	-0.80	2.31	-0.34

Notes: Analysis over period December 31, 1994 to February 28, 2018. Annualized statistics based on monthly data. Returns gross of transaction costs. \* Sharpe ratios statistically significant at the 5% confidence level after adjusting for selection bias under multiple testing.

when hedging other exposures. Finally, the liquidity factor experienced negative excess returns over our testing period, confirming the low liquidity premium reported in other empirical studies.

Another challenge in evaluating the results of strategy backtests reported in the literature is the lack of information regarding the number of tests conducted and the potential impact of these multiple tests on the statistical significance of the reported results. In the Appendix, we use a new template proposed by Fabozzi and Prado (2018) to assess the potential impact of selection bias under multiple testing. We find that the relevant Sharpe ratio cutoff point for the backtests reported in Exhibit 1 is 0.57 at the 5% level of significance. By using this cutoff, we see that the Sharpe ratios of 10 of the 16 factors constructed through multivariate regression were significant after adjusting for selection bias.

Using a consistent point-in-time global dataset and different factor return estimation methods, we broadly confirmed the existence of positive excess returns associated with the main equity factors reported in the literature. But can investors capture these excess returns in practice? How would the introduction of factors affect the performance and characteristics of different investment strategies? Would the introduction of factor tilts reduce the investability and diversification benefits of index strategies? Can factors enhance active strategies without impairing the manager's ability to select stocks and generate alpha? In the next sections, we use the Black–Litterman framework to show how factors can be integrated in standard market indexes and in actual long-only discretionary portfolios.

#### INTEGRATING FACTORS IN MARKET INDEXES

Black and Litterman (1992) introduced a general framework for combining market information and active investor views in a consistent manner to construct global fixed-income and multiasset class portfolios. In a subsequent study, He and Litterman (1999) showed that an unconstrained optimal portfolio that combines market views and investor views can be written simply as the sum of market portfolio weights and the weights of different view portfolios.

Jones, Lim, and Zangari (2007) investigated how the Black–Litterman framework can be applied in the management of quantitative strategies. In this setting, equilibrium returns are combined with view portfolios that are based on quantitative factors. They discussed various methods for constructing view portfolios based on factor information. We use two approaches similar to those used by Jones, Lim, and Zangari to introduce factor information into an index. In the first approach, the index represents the market view portfolio that we modify by incorporating factor information captured in factor view portfolios:

$$\boldsymbol{b}^* = \boldsymbol{b} + \boldsymbol{c} \cdot \boldsymbol{P'} \boldsymbol{w} \tag{1}$$

where  $b^*$  is a vector containing modified index weights, b is a vector containing initial index weights, P is a matrix with rows containing the weights of factor view portfolios, w is a vector of weights on the factor view portfolios, and c is a scaling parameter. In the second approach, we tilt the index toward factors to ensure we do not remove any index constituents, and we avoid short positions:

$$\boldsymbol{b}^* = \boldsymbol{b} + c \cdot diag(\boldsymbol{b}) \boldsymbol{P'w} \tag{2}$$

The next challenge is to translate factor information into view portfolios P. We can use univariate and multivariate cross-sectional regression to derive factor view portfolio weights. In the univariate regression case, asset returns comprise factor and specific components:

$$\boldsymbol{r} = \boldsymbol{x}f + \boldsymbol{e} \tag{3}$$

where r is a vector containing asset excess returns, x is a vector containing asset exposures to the single factor, f is the target factor return, and e is a vector of specific returns. In this case, the weights of the factor view portfolio are simply the security exposures to the target factor, scaled by a constant:

$$f = (\mathbf{x}'\mathbf{x})^{-1}\mathbf{x}'\mathbf{r} = k\mathbf{x}'\mathbf{r} = \mathbf{p}'\mathbf{r}$$
(4)

In the multivariate case, asset returns are driven by multiple factors and specific return sources:

$$\boldsymbol{r} = \boldsymbol{X}\boldsymbol{f} + \boldsymbol{e} \tag{5}$$

where X is now a matrix containing asset exposures to the multiple factors and f is a vector of factor returns. In this case, the factor-view portfolio weights are the weights of pure factor portfolios that have unit exposure to the target factor, zero exposure to all other factors, and minimum specific risk:

$$\boldsymbol{f} = (\boldsymbol{X}'\boldsymbol{X})^{-1}\boldsymbol{X}'\boldsymbol{r} = \boldsymbol{P}\boldsymbol{r}$$
(6)

Pure factor portfolios are difficult to implement in practice because they typically contain a large number of holdings, have both long and short positions, and experience high portfolio turnover. Melas, Suryanarayanan, and Cavaglia (2010) explored different methods for implementing factor portfolios with fewer holdings and limited turnover. The factor integration methods we investigate in this study do not require pure factor portfolios to be replicated; these portfolios are only used as input to reweight broad market indexes.

We apply these methods to reweight the MSCI ACWI IMI index and three main regional indexes. We use factor exposure data from MSCI's Global Equity Model for Long-Term Investors to derive the factor portfolio weights. We assign equal weights to the factors, winsorize factor exposures at three standard deviations, limit factor portfolio weights at  $\pm 3\%$ , and set parameter *c* at levels that result in active risk of approximately 50 bps. We test four methods of integrating factors into market indexes:

- 1. Add method (Equation 1), using view portfolio weights based on factor exposures (Equation 4)
- 2. Tilt method (Equation 2), using view portfolio weights based on factor exposures (Equation 4)

- 3. Add method (Equation 1), using view portfolio weights based on factor portfolios (Equation 6)
- 4. Tilt method (Equation 2), using view portfolio weights based on factor portfolios (Equation 6)

We use these four methods to modify the index weights by combining them with factor information and compare the performance and investability characteristics of the parent and modified indexes. Exhibit 2 shows that factor-tilted indexes outperformed the parent cap-weighted indexes in the four regions and the historical period we examined, across both portfolio construction methods (add, tilt) and both factor return estimation methods (univariate, multivariate). The add method (Equation 1) in particular achieved superior performance, whereas the tilt method (Equation 2) had better investability. Furthermore, we observe that the add method worked particularly well when pure factor portfolio weights were used as the factor view portfolios.

As expected, the factor exposures of the reweighted indexes move toward target factors by small amounts. Even though all methods led to approximately the same active risk, add methods achieved more aggressive factor tilts, better absolute and relative risk-adjusted performance, and higher attribution to factors (shaded row in Exhibit 2). Active return attributed to other sources remained generally low across all methods, confirming that no significant unintended exposures or biases were introduced to the indexes as a result of the reweighting process.

Although add methods, especially when using pure factor portfolio weights, had superior performance, tilt methods led to better investment capacity because they are anchored to the market cap weights of the parent indexes. Add methods also removed approximately 10% of the holdings of the parent index and had slightly lower market cap coverage and moderately higher average ownership as percentage of company float market capitalization. Finally, add methods required higher turnover and would take longer to trade the index around rebalancing for a certain level of assets under management.

All factor integration methods we investigated improved the risk-adjusted performance of market indexes historically. For investors with low or moderate assets under management that can accept a small deterioration in index capacity and liquidity, the add method that combines index weights and pure factor portfolios was the most efficient way of integrating factor information into an index. This method achieved historical IRs ranging between 0.9 and 1.9 over our sample period. On the other hand, investors managing large index-tracking portfolios may opt for the tilt method that uses factor exposures to reweight the index. This approach achieved lower, albeit still impressive, historical performance while leaving index investability characteristics virtually unchanged.

#### INTEGRATING FACTORS IN DISCRETIONARY STRATEGIES

In the previous sections, we confirmed the existence of long-term factor premiums in global equities and examined ways of integrating factor information into market indexes. We found that tilting indexes toward factors improved risk-adjusted performance without reducing liquidity, investability, and diversification. In this section, we turn to the question of incorporating factor views into discretionary strategies. In these strategies, portfolio managers may have concerns that adding factor tilts may distort their investment process and affect their ability to generate alpha from stock selection.

To address these concerns and avoid substantial changes to an existing discretionary portfolio, we incorporate factors by reweighting portfolio holdings. This method ensures that all existing securities remain in the portfolio after the integration of factor views, albeit with modified weights. Effectively, through this process we do not add or remove any names from the portfolio. We only reweight the existing securities picked by the manager to introduce tilts toward rewarded factors. We use two sets of factor-related signals to reweight the portfolio, factor exposures (Equation 4) and factor alpha, calculated using each factor's historical IR and current forecast risk:

$$\boldsymbol{\alpha}_{i,k} = \boldsymbol{x}_{i,k} \boldsymbol{\sigma}_k \boldsymbol{\omega}_k \tag{7}$$

where  $\alpha_{i,k}$  is the factor alpha of security *i* coming from its exposure to factor *k*,  $x_{i,k}$  is the exposure of security *i* to factor *k*,  $\sigma_k$  is the forecast risk of factor *k*, and  $\omega_k$  is the historical factor IR. In total, we tested three ways of modifying the weights of a discretionary portfolio using factor data:

1. Add method (Equation 1), using view portfolio weights based on factor exposures (Equation 4)

			V	<b>CWI IM</b>	=			Nort	h Ameri	ica				EAFE				Emerg	ging Ma	rkets	
NCC 1011 listo         Idia		MSCI	Univ	ariate	Multiv	ariate	MSCI	Univa	riate	Multiv:	ariate	MSCI	Univa	riate	Multiv	ariate	MSCI	Univa	riate	Multiv	ariate
	<b>MSCI IMI Indexes</b>	Index	Add	Tilt	$\mathbf{A}$ dd	Tilt	Index	bbA	Tilt	bbA	Tilt	Index	ppy	Tilt	bbA	Tilt	Index	ppy	Tilt	ppy	Tilt
Induction         5         5         5         7         1         5         1         5         1         5         1         5         1         5         1	<b>Absolute Performance</b>																				
Numerikanis         155         151 <th< td=""><td>Total Return (%)</td><td>6.23</td><td>6.65</td><td>6.52</td><td>7.13</td><td>6.50</td><td>6.60</td><td>6.87</td><td>6.85</td><td>7.02</td><td>6.67</td><td>5.34</td><td>5.86</td><td>5.81</td><td>6.12</td><td>5.71</td><td>9.70</td><td>10.2</td><td>10.2</td><td>10.6</td><td>10.2</td></th<>	Total Return (%)	6.23	6.65	6.52	7.13	6.50	6.60	6.87	6.85	7.02	6.67	5.34	5.86	5.81	6.12	5.71	9.70	10.2	10.2	10.6	10.2
Member beine prefame         0.27         0.39         0.35         0.33<	Volatility (%)	15.5	15.2	15.2	15.3	15.6	15.1	14.7	14.7	14.8	15.0	16.5	16.2	16.2	16.3	16.6	22.2	21.9	21.9	21.9	22.1
Retain Retain Tracking Error (%)0.30	Sharpe Ratio	0.27	0.30	0.29	0.33	0.28	0.30	0.32	0.32	0.33	0.30	0.20	0.23	0.23	0.25	0.22	0.34	0.37	0.37	0.39	0.36
Active lenge         0.2         0.3 <t< td=""><td><b>Relative Performance</b></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>	<b>Relative Performance</b>																				
	Active Return (%)		0.42	0.29	0.90	0.27		0.27	0.25	0.42	0.07		0.52	0.47	0.78	0.37		0.54	0.46	0.90	0.45
Information Infor	Tracking Error (%)		0.53	0.43	0.47	0.54		0.60	0.54	0.49	0.55		0.49	0.56	0.46	0.57		0.54	0.57	0.54	0.59
Alter in the second of	Information Ratio		0.78	0.66	1.92	0.51		0.44	0.47	0.86	0.12		1.05	0.84	1.71	0.65		1.01	0.81	1.65	0.76
Male         001         002         001         001         002         002         003 </td <td>Act Factor Exposures</td> <td></td>	Act Factor Exposures																				
	Value		0.03	0.01	0.05	0.01		0.02	0.01	0.01	0.00		0.03	0.02	0.04	0.03		0.03	0.03	0.05	0.02
	Size		-0.04	-0.03	-0.15	-0.07		-0.02	-0.02	-0.09	-0.02		-0.06	-0.06	-0.14	-0.11		-0.02	-0.03	-0.06	-0.05
Walatily $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-004$ $-003$ $-$	Momentum		0.01	0.01	0.06	0.04		0.01	0.01	0.05	0.03		0.02	0.02	0.05	0.03		0.02	0.02	0.04	0.03
	Volatility		-0.04	-0.04	-0.05	-0.02		-0.04	-0.04	-0.03	-0.01		-0.04	-0.06	-0.05	-0.02		-0.03	-0.03	-0.03	-0.01
Vield004003008005003003004003004003004003004003004003004003004003004003004003004003 <th< td=""><td>Quality</td><td></td><td>0.02</td><td>0.02</td><td>0.02</td><td>0.01</td><td></td><td>0.01</td><td>0.02</td><td>0.00</td><td>0.00</td><td></td><td>0.03</td><td>0.03</td><td>0.02</td><td>0.00</td><td></td><td>0.02</td><td>0.02</td><td>0.03</td><td>0.01</td></th<>	Quality		0.02	0.02	0.02	0.01		0.01	0.02	0.00	0.00		0.03	0.03	0.02	0.00		0.02	0.02	0.03	0.01
	Yield		0.04	0.03	0.08	0.05		0.03	0.03	0.06	0.03		0.04	0.03	0.05	0.04		0.04	0.04	0.07	0.05
	Growth		0.01	0.00	0.07	0.04		0.00	-0.01	0.05	0.02		0.02	0.02	0.06	0.05		0.02	0.01	0.05	0.04
Active Attribution (%)Active Attribution (%)Currencies $-011$ $-001$ $-001$ $-001$ $-002$ $-002$ $-003$ $-002$ $-003$ $-002$ $-003$ $-002$ $-003$ $-002$ $-003$ $-002$ $-003$ $-002$ $-003$ $-002$ $-003$ $-002$ $-003$ $-002$ $-003$ $-002$ $-003$ $-003$ $-001$	Liquidity		-0.05	-0.02	-0.08	-0.02		-0.03	-0.02	-0.04	-0.02		-0.06	-0.04	-0.09	-0.03		-0.04	-0.03	-0.05	-0.02
	Active Attribution (%)																				
	Currencies		-0.01	-0.01	0.02	0.01		0.00	0.00	0.00	0.00		0.01	0.00	-0.01	-0.04		-0.02	-0.03	-0.02	-0.01
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	Countries		-0.01	-0.02	0.02	0.00		0.00	-0.01	0.00	0.01		0.03	-0.01	0.05	0.00		-0.01	-0.04	0.03	0.02
	Industries		-0.03	-0.01	0.01	0.01		-0.06	-0.04	0.00	0.00		0.01	0.03	0.02	0.00		0.06	0.03	0.05	-0.01
	Factors		0.49	0.32	0.87	0.42		0.37	0.32	0.55	0.25		0.52	0.44	0.72	0.44		0.42	0.40	0.66	0.34
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	Specific		-0.02	0.01	-0.02	-0.16		-0.05	-0.01	-0.13	-0.19		-0.04	0.01	0.00	-0.03		0.09	0.10	0.17	0.11
	Total Active		0.42	0.29	06.0	0.27		0.27	0.25	0.42	0.07		0.52	0.47	0.78	0.37		0.54	0.46	06.0	0.45
Avg. No. of Stocks         8,894         7,979         8,883         7,608         8,833         7,608         8,833         7,608         8,833         7,608         8,833         7,608         8,833         7,608         2,971         3,556         3,552         3,516         2,203         2,306         2,173         2,39         331         2,316         2,203         2,306         2,173         2,93         331         2,317         2,03         2,316         2,133         2,306         2,173         2,93         331         2,317         2,03         2,04         9,47         9,47         9,17         100         9,11         0,11         0,11         0,11         0,11         0,13         0,14         0,03         0,06         0,10         0,06         0,16         0,18         0,16         0,18         0,11         0,11         0,11         0,11         0,13         0,14         0,03         0,06         0,10         0,06         0,16         0,18         0,11         0,21         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0,31         0	Investment Capacity																				
Effect. No. of Stocks534544539587516208209217198300307312325331207208214213213MCap Coverage (%)10099.299.897899.810099.199.799.799.799.799.199.199.199.199.1Awg. Own (% Float)0.020.030.040.030.040.050.040.050.040.050.060.160.160.180.160.130.10Max. Own (% Float)0.020.030.040.030.040.650.040.650.040.050.060.160.160.180.160.130.10Max. Own (% Float)0.020.030.030.030.040.050.040.650.040.050.060.160.180.160.180.10Max. Own (% Float)0.020.030.030.030.270.040.650.040.050.060.160.180.160.180.10Max. Own (% Float)0.0097.467.41.01.001.501.101.001.301.101.301.10Max. Det with filter1.0097.467.515.416.61.211.201.201.001.301.10Max. Det with filter1.0097.467.61.5715.416.61.2112.01.201.201.	Avg. No. of Stocks	8,894	7,979	8,883	7,608	8,883	2,982	2,749	2,971	2,598	2,971	3,596	3,259	3,562	3,278	3,562	2,316	2,203	2,306	2,159	2,306
	Effect. No. of Stocks	534	544	539	587	516	208	209	209	217	198	300	307	312	325	331	207	208	214	213	213
Avg. Own (% Float) $0.02$ $0.03$ $0.02$ $0.03$ $0.02$ $0.03$ $0.04$ $0.03$ $0.06$ $0.10$ $0.06$ $0.16$ $0.16$ $0.16$ $0.16$ $0.16$ $0.16$ $0.11$ $0.21$ $0.17$ Max. Own (% Float) $0.02$ $0.33$ $0.47$ $0.03$ $0.03$ $0.27$ $0.04$ $0.65$ $0.06$ $0.10$ $0.06$ $0.16$ $0.11$ $0.21$ $0.17$ Max. Own (% Float) $0.02$ $0.33$ $0.27$ $0.04$ $0.65$ $0.04$ $0.26$ $0.06$ $0.16$ $0.16$ $0.11$ $0.21$ $1.08$ $1.10$ Awg. Wgt. Multiplier $1.00$ $9.74$ $6.03$ $1.26$ $1.21$ $1.10$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.30$ $1.10$ $1.30$ $1.10$ $1.30$ $1.10$ $1.30$ $1.10$	MCap Coverage (%)	100	99.2	8.66	97.8	8.66	100	99.4	8.66	98.4	8.66	100	99.1	7.66	98.7	7.66	100	99.1	99.4	98.7	99.4
Max. Unit for the formation         0.02         0.02         0.02         0.02         0.02         0.02         0.02         0.02         0.02         0.02         0.02         0.02         0.02         0.01         <	Avg. Own (% Float)	0.02	0.03	0.02	0.04	0.02	0.03	0.04	0.03	0.06	0.03	0.06	0.08	0.06	0.10	0.06	0.16	0.18	0.16	0.21	0.17
Avg. Wgt. Multiplier1.00 $1.50$ $1.10$ $1.00$ $1.50$ $1.10$ $1.00$ $1.50$ $1.10$ $1.00$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ $1.00$ $1.10$ <	Index Concentration	70.0	0000	CO.0	- <del>-</del> - 0	CO.0	CO.0	17.0	5.0	CO.0	+0.0	00	10.0	60.0	00.00	60.0	01.0	+	17.0	1.00	17.0
Way: Weit Multiplier       1.00       7.45       7.46       7.47       1.50       1.41       1.60       1.42       1.70       1.00       8.8       1.4       9.3       3.3       3.3       3.4       0.00       3.0       3.40       6.9       6.90 <td>Avg Wot Multiplier</td> <td>1 00</td> <td>1 50</td> <td>1 10</td> <td>2 10</td> <td>1 10</td> <td>1 00</td> <td>1 30</td> <td>1 10</td> <td>1 60</td> <td>1 00</td> <td>1 00</td> <td>1 50</td> <td>1 10</td> <td>1 80</td> <td>1 20</td> <td>1 00</td> <td>1 10</td> <td>1 00</td> <td>1 30</td> <td>1 10</td>	Avg Wot Multiplier	1 00	1 50	1 10	2 10	1 10	1 00	1 30	1 10	1 60	1 00	1 00	1 50	1 10	1 80	1 20	1 00	1 10	1 00	1 30	1 10
Top 10 Sec. Wgs. (%)       8.40       8.50       8.10       9.30       15.7       15.6       15.7       15.4       16.6       12.1       11.8       11.7       16.2       16.2       15.9       16.0       16.0         Max. Index Wgt. (%)       1.50       1.50       1.50       1.50       1.50       1.50       1.50       1.60       16.0<	Max Wot Multiplier	1 00	97.4	60.2	122	613	1 00	80.9	603	74.6	57.4	1 0	141	1 60	14.8	1 70	1 0	88	14	8.6	14
Mar. Index Wet. (%)         1.50         3.20         3.20         3.30         3.40         6.90 </td <td>Top 10 Sec. Wets. (%)</td> <td>8.40</td> <td>8.40</td> <td>8.50</td> <td>8.10</td> <td>9.30</td> <td>15.7</td> <td>15.6</td> <td>15.7</td> <td>15.4</td> <td>16.6</td> <td>12.1</td> <td>12.0</td> <td>12.1</td> <td>11.8</td> <td>11.7</td> <td>16.2</td> <td>16.2</td> <td>15.9</td> <td>16.0</td> <td>16.0</td>	Top 10 Sec. Wets. (%)	8.40	8.40	8.50	8.10	9.30	15.7	15.6	15.7	15.4	16.6	12.1	12.0	12.1	11.8	11.7	16.2	16.2	15.9	16.0	16.0
$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	Max. Index Wgt. (%)	1.50	1.50	1.50	1.40	1.60	2.80	2.80	2.80	2.70	2.90	1.80	1.80	1.80	1.70	1.90	3.30	3.30	3.20	3.30	3.40
Index Replicability           Annual Turnover         4.20         6.90         5.90         16.0         13.0         13.0         13.6         10.7         12.9         12.4         16.5         16.0           Annual Turnover         4.20         6.90         5.90         10.0         0.40         0.20         0.40         0.50         13.0         13.6         10.7         12.9         12.4         16.5         16.0           Day to Trade 95%         0.20         0.30         0.10         0.40         0.20         0.40         0.50         0.30         0.60         0.70         1.30         0.70         2.00         0.70           Day to Trade 95%         0.20         0.30         0.10         0.40         0.20         0.40         0.50         0.40         0.70         1.30         0.70         2.00         0.70           Day to Trade Max         1.00         7.60         1.00         14.4         1.10         0.50         2.20         0.50         1.40         3.60         1.40         7.60         1.00         7.70         31.9         8.10	Active Share (%)	0.00	3.50	2.80	12.1	11.0	0.00	2.40	2.70	8.80	6.80	0.00	4.20	4.60	9.70	11.3	0.00	3.00	3.40	6.90	6.90
Annual Turnover       4.20       6.90       5.90       16.0       14.5       3.30       5.30       5.00       13.0       10.4       4.20       7.20       13.0       13.6       10.7       12.9       12.4       16.5       16.0         Day to Trade 95%       0.20       0.30       0.10       0.40       0.20       0.40       0.50       0.30       0.60       0.40       0.70       13.0       13.0       13.0       13.0       0.70       2.00       0.70         Day to Trade 95%       0.20       0.30       0.50       0.40       0.70       13.0       0.70       2.00       0.70         Days to Trade Max       1.00       7.60       1.01       0.50       2.20       0.50       1.40       3.60       1.40       4.60       1.67       12.9       12.4       16.5       16.0         Days to Trade Max       1.00       7.60       1.00       14.4       1.10       0.50       2.20       0.50       1.40       3.60       1.40       4.60       1.60       7.50       20.2       8.10       17.9       13.9       8.10	Index Replicability																				
Day to Trade 95%       0.20       0.30       0.10       0.40       0.10       0.20       0.40       0.50       0.40       0.50       0.70       2.00       0.70         Days to Trade Max       1.00       7.60       1.00       14.4       1.10       0.50       2.20       0.60       4.20       0.50       1.40       3.60       1.40       4.60       1.60       7.50       20.2       8.10       31.9       8.10	Annual Turnover	4.20	6.90	5.90	16.0	14.5	3.30	5.30	5.00	13.0	10.4	4.20	7.20	7.20	13.0	13.6	10.7	12.9	12.4	16.5	16.0
Days to Trade Max 1.00 7.60 1.00 14.4 1.10 0.50 2.20 0.60 4.20 0.50 1.40 3.60 1.40 4.60 1.60 7.50 20.2 8.10 31.9 8.10	Day to Trade 95%	0.20	0.30	0.10	0.40	0.10	0.20	0.40	0.20	0.50	0.20	0.40	0.50	0.30	0.60	0.40	0.70	1.30	0.70	2.00	0.70
	Days to Trade Max	1.00	7.60	1.00	14.4	1.10	0.50	2.20	0.60	4.20	0.50	1.40	3.60	1.40	4.60	1.60	7.50	20.2	8.10	31.9	8.10

2

EXHIBIT

- 2. Tilt method (Equation 2), using view portfolio weights based on factor exposures (Equation 4)
- 3. Tilt method (Equation 2), using view portfolio weights based on factor alpha (Equation 7)

We tested these methods of integrating factors in active portfolios on a universe of 1,182 global and international (global ex US) actively managed mutual funds during the period December 2008 to December 2017. We assess the impact of factor tilts across all active funds but also within groups of funds sorted on historical performance. We reweight the active portfolios in our dataset using factor exposure and factor alpha information on a monthly basis. Exhibit 3 shows the historical performance of these active mutual fund portfolios before and after the integration of factor tilts.

The original portfolios (first shaded column in Exhibit 3) achieved average outperformance of 0.73% with an IR of 0.17. Factor exposures were generally modest, with small positive tilts to quality and momentum and negative tilts to size and yield. Most of the outperformance came from security selection (27 bps), whereas countries and industries each contributed 20 bps. Stock selection made the highest contribution across all four performance quartiles in the original active portfolios.

Modified portfolios based on adding factor exposures (second shaded column in Exhibit 3) achieved outperformance of 1.48% with IR of 0.35: Adding factors improved performance substantially both in absolute and risk-adjusted terms. Factor exposures show that the factor profile of these active funds moved toward rewarded factors. Performance attribution confirms that all the added active return came from factor tilts that we introduced to the portfolios. Interestingly, performance attributed to security selection remained virtually unchanged at 27 bps before and 26 bps after the factor tilts. Thus, tilting the portfolios toward rewarded factors added 75 bps to active return without affecting the specific contribution.

Modified portfolios using factor exposures to tilt the original portfolio weights (third shaded column in Exhibit 3) achieved even better results, adding 90 bps to active returns on average and increasing the IR from 0.17 to 0.39. This was achieved through slightly more aggressive tilting of original portfolios to rewarded factors. This approach also left the managers' stock selection contribution unchanged.

Portfolios tilted on factor alpha (see fourth shaded column in Exhibit 3) outperformed by 1.53% on average with an IR of 0.34. Using factor alpha to tilt the original portfolios did improve performance roughly in line with the other methods. However, using factor alpha had a negative impact on the specific contribution, which declined from 26 to 13 bps on average. Furthermore, the tilts required higher portfolio turnover to implement, compared to the other methods. Transforming exposures into alphas using Equation 7 favors factors that have a higher IR and higher forecast volatility because factor alpha is proportional to the product of factor IR and factor volatility. Exhibit 1 shows that value and momentum are the two factors that score highly on this measure. Indeed Exhibit 3 confirms that we achieve more aggressive tilts toward these two factors when we use factor alpha.

These results suggest that using exposures to tilt active portfolios may be the preferred approach for managers who wish to maintain their security selection contribution and benefit from factor premiums. Indeed, irrespective of manager skill prior to the integration of factors, all four quartiles experienced substantial uplift in performance while their specific return contribution remained unchanged. On the other hand, factor alphas may be preferred inputs for certain managers-for example, those who use explicit return forecasts in their process as inputs to optimized portfolio construction or those who wish to place more emphasis on factors with a higher historical IR and higher forecast volatility. Using factor alphas to tilt active portfolios resulted in performance benefits but also led to a small reduction in specific returns.

#### INTEGRATING FACTORS IN DISCRETIONARY STRATEGIES: A PRACTICAL EXAMPLE

In this section, we show an example of how to incorporate factors in a specific active portfolio from our database. For illustration, we select the exposure-based tilt method; the other methods proceed similarly. The original and modified portfolio weights and some of the intermediate calculations are presented in Exhibit 4.

The fund in question had 46 stocks as of December 31, 2017, with 63% invested in the United States, 13% in the United Kingdom, and 24% in other markets. The fund had the largest sector weights in the information technology, consumer discretionary, and

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		Origiı	nal Porti	folios			Modifi	ed Portf	olios			Modif	ied Port	folios			Modifi	ed Portfo	lios	
Historical Performance of	ŝ	Y Perfor	) mance (	Quartiles		Add	Methoo	l, Factor	Exposu	re	Tilt	Method	l, Factor	· Exposu	re	L	<b>Jilt Metho</b>	d, Factor	Alpha	
<b>Global Equity Funds</b>	01	Q2	<b>Q</b> 3	Q4	IIV	Q1	Q2	63	Q4	Ш	Q1	Q2	<b>0</b> 3	Q4	All	Q1	Q2	<b>Q</b> 3	Q4	IIV
Absolute Performance													:							
Total Return (%)	3.55	5.47	6.47	9.28	6.19	4.35	6.21	7.23	10.0	6.94	4.53	6.38	7.40	10.1	7.09	4.44	6.23	7.22	10.1	6.99
Volatility (%)	18.8	17.9	18.1	18.5	18.3	18.1	17.2	17.4	17.9	17.7	17.9	17.1	17.3	17.8	17.5	18.5	17.7	17.9	18.4	18.1
Sharpe Ratio Perf. Rel. to Benchmark	0.26	0.38	0.43	0.57	0.41	0.32	0.44	0.49	0.63	0.47	0.33	0.45	0.50	0.64	0.48	0.31	0.43	0.48	0.62	0.46
Active Return (%)	-2.35	-0.04	1.28	4.06	0.73	-1.55	0.70	2.03	4.76	1.48	-1.37	0.86	2.20	4.86	1.63	-1.46	0.72	2.02	4.86	1.53
Tracking Error (%)	5.06	3.95	4.13	5.61	4.68	4.90	3.91	4.12	5.53	4.61	4.89	3.95	4.17	5.54	4.64	5.02	4.05	4.28	5.70	4.76
Information Ratio	-0.46	-0.01	0.35	0.79	0.17	-0.30	0.20	0.56	0.95	0.35	-0.26	0.25	0.60	0.96	0.39	-0.28	0.19	0.52	0.92	0.34
Perf. Rel. to Original Port.																				
Active Return (%)						0.80	0.74	0.76	0.70	0.75	0.98	0.90	0.92	0.80	0.90	0.88	0.76	0.74	0.79	0.80
Tracking Error (%) Information Datio						1.15	1.12	1.09	1.17 0.50	1.14	1.40	1.35	1.34 0.60	1.40	1.37	1.18	1.15	1.15	1.21	1.17
Day from Original Dart							0	2	2		2					2			2	2
Dev. Irom Original Fort.									100					0000	000				1 0 0	
Avg. Active Wgt. (%) Max Active Wgt. (%)						0.28	0.26 0.85	0.26 0.83	0.34 1.08	0.28	0.32 1.36	0.30	0.30 1.29	0.38	0.33 1.37	0.31 1.30	0.28	0.28 1.23	0.35	0.31
Active Share (%)						9.70	10.00	9.86	10.3	9.96	11.4	11.9	11.8	12.0	11.8	10.6	11.0	10.9	11.0	10.9
Portfolio Jurnover																				
Total Turnover (%, pa) Incre. Turnover (%, pa)	71.1	66.3	63.6	63.3	66.1	87.8 16.7	84.3 18.0	81.4 17.8	82.2	84.0	90.9 19.9	87.9 21.6	85.3 21.7	85.9 22.6	87.5 ] 21.4	40.1	108.5 ] 42.2	41.4	106.0 1 42.7	07.7 41.6
Active Factor Exposures																				
Value	0.02	0.01	-0.04	-0.13	-0.04	0.03	0.02	-0.03	-0.11	-0.02	0.03	0.02	-0.03	-0.11	-0.02	0.06	0.05	0.00	-0.09	0.01
Size	-0.25	-0.18	-0.23	-0.38	-0.26	-0.32	-0.24	-0.30	-0.46	-0.33	-0.32	-0.25	-0.30	-0.47	-0.33	-0.27	-0.21	-0.25	-0.41	-0.29
Momentum	-0.02	0.03	0.07	0.11	0.05	0.02	0.07	0.11	0.15	0.09	0.03	0.07	0.12	0.16	0.09	0.05	0.10	0.14	0.18	0.12
Volatility	0.07	0.05	0.04	-0.02	0.04	-0.04	-0.06	-0.06	-0.12	-0.07	-0.06	-0.08	-0.09	-0.14	-0.09	0.08	0.06	0.05	-0.01	0.04
Quality	0.03	0.04	0.07	0.10	0.06	0.13	0.14	0.17	0.20	0.16	0.15	0.16	0.19	0.22	0.18	0.08	0.08	0.11	0.15	0.10
Yield	-0.07	-0.09	-0.14	-0.23	-0.13	0.00	-0.03	-0.08	-0.17	-0.07	0.01	-0.01	-0.06	-0.16	-0.06	-0.04	-0.06	-0.11	-0.21	-0.10
Growth	0.03	0.04	0.07	0.13	0.07	0.05	0.06	0.09	0.15	0.09	0.05	0.06	0.09	0.15	0.09	0.04	0.05	0.08	0.13	0.07
Liquidity	0.05	0.04	0.04	0.01	0.04	0.00	-0.01	-0.01	-0.05	-0.02	-0.01	-0.03	-0.02	-0.06	-0.03	0.05	0.04	0.04	0.01	0.04
Active Attribution (%)																				
Styles	-0.45	0.05	0.28	0.66	0.13	0.23	0.73	0.96	1.36	0.82	0.35	0.85	1.08	1.48	0.94	0.42	06.0	1.13	1.54	1.00
Industries	-0.41	0.00	0.28	0.89	0.19	-0.32	0.09	0.35	0.90	0.25	-0.29	0.12	0.38	06.0	0.28	-0.34	0.05	0.34	0.93	0.24
Countries	-0.28	0.21	0.34	0.59	0.21	-0.26	0.24	0.39	0.62	0.24	-0.26	0.24	0.39	0.62	0.25	-0.31	0.20	0.33	0.59	0.20
Currencies	-0.30	-0.06	-0.01	0.08	-0.07	-0.31	-0.08	-0.03	0.08	-0.08	-0.32	-0.09	-0.04	0.08	-0.09	-0.26	-0.03	0.01	0.14	-0.04
Specific	-0.89	-0.24	0.39	1.84	0.27	-0.87	-0.27	0.37	1.81	0.26	-0.84	-0.26	0.38	1.78	0.26	-0.96	-0.40	0.22	1.66	0.13
Total Active	-2.35	-0.04	1.28	4.06	0.73	-1.55	0.70	2.03	4.76	1.48	-1.37	0.86	2.20	4.86	1.63	-1.46	0.72	2.02	4.86	1.53

Note: Analysis over period December 31, 2008 to December 31, 2017 using holdings of 1,182 global and international actively managed mutual funds.

Holding Name	Original Weight	Factor Alpha	Multiplier	Weight* Multiplier	Rescaled Weight	Value	Size	Momentum	Volatility	Quality	Yield	Growth	Liquidity
VERIZON COMMUNICATIONS INC	5.7%	0.18	1.11	6.3%	4.9%	0.48	0.93	-0.15	-0.66	-0.43	1.51	-0.97	-0.65
NOSNHOL & NOSNHOL	5.2%	0.59	1.34	7.0%	5.4%	0.04	0.93	0.28	-1.01	0.65	0.38	-0.40	-1.00
MICROSOFT CORP	4.7%	-0.09	0.95	4.5%	3.5%	-0.41	0.93	0.49	0.16	0.33	0.12	-0.11	-0.68
PFIZER INC	4.6%	0.65	1.38	6.3%	4.9%	0.43	0.93	-0.07	-0.77	0.72	1.11	-0.55	-0.74
WH SMITH PLC	4.2%	1.24	1.72	7.2%	5.6%	-0.67	-1.74	0.58	-1.15	2.38	-0.86	-0.41	0.55
AT&T INC	3.9%	0.52	1.30	5.0%	4.0%	0.77	0.93	-0.51	-0.85	0.02	1.90	-0.56	-0.32
CISCO SYS INC	3.9%	0.27	1.15	4.5%	3.5%	0.42	0.93	0.37	-0.22	0.21	0.77	-0.35	-0.37
INTERNATIONAL BUSINESS MACHS	3.7%	0.16	1.10	4.0%	3.1%	0.76	0.93	-0.66	-0.34	0.61	1.24	-0.89	-0.29
TOTAL	3.4%	0.15	1.08	3.7%	2.9%	0.52	1.06	-0.49	0.10	0.27	1.39	-0.36	0.22
SAMSUNG ELECTRONICS CO LTD	3.2%	0.51	1.30	4.2%	3.3%	0.51	1.74	0.74	0.79	1.22	0.22	0.71	-0.71
MAYR MELNH OF KARTONORD	3.2%	1.43	1.83	5.9%	4.6%	-0.09	-0.82	0.00	-0.47	1.01	-0.08	-0.18	-2.07
WALGREENS BOOTS ALLIANCE INC	3.2%	-0.13	0.92	2.9%	2.3%	0.49	0.48	-1.13	-0.81	0.17	0.25	0.17	0.39
ANTHEM INC	3.1%	0.62	1.36	4.3%	3.4%	0.36	0.30	1.03	-0.07	1.12	-0.31	0.03	-0.14
GAP INC DEL	3.1%	0.91	1.53	4.8%	3.7%	0.52	-0.94	1.10	0.75	2.21	0.51	-0.44	1.11
CVS HEALTH CORP	3.1%	0.18	1.10	3.4%	2.7%	1.08	0.50	-0.92	-0.64	0.45	0.66	-0.39	0.22
CHEVRON CORP NEW	2.7%	1.04	1.61	4.3%	3.4%	-0.08	0.93	0.08	-0.68	0.44	0.95	1.64	-0.63
KDDI	2.6%	0.24	1.14	2.9%	2.3%	0.44	1.28	-0.32	0.09	0.66	0.80	-0.36	-0.31
APPLE INC	2.6%	0.02	1.01	2.6%	2.0%	0.28	0.93	0.66	-0.06	0.03	-0.15	0.21	-0.17
RCL FOODS LIMITED	2.3%	1.93	2.00	4.6%	3.6%	0.98	-1.98	-0.79	0.25	0.03	-0.26	0.66	-2.84
ORACLE CORPORATION	2.2%	-0.22	0.87	1.9%	1.5%	0.35	0.93	-0.06	-0.06	0.00	-0.11	-0.39	-0.69
CHINA MOBILE LTD	2.0%	0.99	1.58	3.2%	2.5%	0.95	0.96	-0.76	-0.69	2.00	1.12	-1.54	-1.44
YOOX NET-A-PORTER GROUP	1.8%	-1.88	0.50	0.9%	0.7%	-1.31	-1.01	-0.86	1.64	-1.63	-1.86	0.70	1.16
TEGNA	1.6%	0.17	1.10	1.8%	1.4%	1.69	-2.05	-0.83	-0.08	-0.31	0.11	-1.04	0.97
DEBENHAMS PLC	1.6%	1.83	2.00	3.2%	2.5%	3.16	-2.78	-2.37	-0.25	1.03	2.21	-1.22	0.70
GLAXOSMITHKLINE	1.5%	-0.11	0.93	1.4%	1.1%	-0.37	0.92	-1.23	-0.61	0.53	1.35	-0.77	-0.13
KINGFISHER	1.5%	0.75	1.43	2.1%	1.7%	0.94	-0.90	-0.35	-0.76	0.94	-0.27	-0.19	0.85
CONNECT GROUP PLC	1.5%	2.41	2.00	2.9%	2.3%	1.33	-3.04	-1.60	-0.20	0.83	2.21	-0.35	-1.19
PALLINGHT	1.4%	0.22	1.13	1.6%	1.3%	0.76	-2.66	-2.09	0.59	-0.72	-1.57	-0.36	-2.02
GANNETT CO INC	1.4%	1.50	1.87	2.6%	2.0%	0.88	-2.55	0.47	0.04	0.95	2.09	-1.17	0.97
UNITEDHEALTH GROUP INC	1.4%	0.56	1.32	1.8%	1.4%	-0.26	0.93	0.93	-0.43	0.92	-0.25	0.40	-0.69

E X H I B I T 4 A Step-by-Step Example of Integrating Factors in a Discretionary Portfolio

	Original	Factor		Weight*	Rescaled								
Holding Name	Weight	Alpha	Multiplier	Multiplier	Weight	Value	Size	Momentum	Volatility	Quality	Yield	Growth	Liquidity
HENKEL STA	1.4%	0.23	1.13	1.6%	1.2%	-0.45	0.36	-0.60	0.17	0.24	-0.52	-0.34	-2.38
EXXON MOBIL CORP	1.3%	0.58	1.33	1.7%	1.3%	0.08	0.93	-0.48	-1.05	0.49	1.09	-0.11	-0.79
INTEL CORP	1.2%	0.24	1.14	1.4%	1.1%	0.62	0.93	0.25	0.23	1.10	0.33	-0.20	-0.03
PERSIMMON	1.2%	0.62	1.36	1.6%	1.2%	0.43	-0.80	0.61	0.21	0.13	0.70	0.08	1.02
CARS.COM	1.1%	0.17	1.10	1.2%	1.0%	0.55	-2.30	-0.10	-0.23	-0.07	-1.02	0.30	1.38
BED BATH & BEYOND INC	1.1%	-0.14	0.92	1.0%	0.8%	2.84	-2.01	-2.36	0.38	1.71	0.52	-2.17	2.32
HEWLETT PACKARD ENTERPRISE	1.1%	-0.11	0.94	1.0%	0.8%	1.04	-0.48	-0.19	0.42	0.97	0.16	-1.72	0.37
SPIRE HEALTHCARE GROUP PLC	1.0%	-0.27	0.85	0.8%	0.6%	0.37	-2.35	-1.85	-0.25	0.31	-1.24	-0.41	0.93
ADIDAS	0.9%	-0.06	0.96	0.9%	0.7%	-1.12	0.14	-0.08	-0.18	0.84	-0.63	0.74	0.49
HP INC	0.8%	0.25	1.14	0.9%	0.7%	0.80	-0.14	0.40	0.47	0.62	0.49	-0.88	0.10
GAZPROM	0.8%	0.25	1.15	0.9%	0.7%	2.01	0.51	-0.76	-0.57	0.22	0.63	-1.41	0.25
DXC TECHNOLOGY	0.7%	1.00	1.58	1.1%	0.9%	-0.03	-0.35	1.00	-0.10	0.85	-0.58	1.59	0.01
VODAFONE GROUP	0.6%	0.80	1.47	0.8%	0.6%	0.04	0.89	-0.08	-0.50	1.47	1.11	-0.15	-0.05
MICRO FOCUS INT	0.3%	-0.41	0.76	0.3%	0.2%	-0.97	-0.60	0.01	-0.43	-1.14	-0.44	0.54	0.60
<b>BIJOU BRIGITTE</b>	0.3%	2.89	2.00	0.6%	0.5%	0.04	-3.00	-0.88	-1.19	1.75	1.82	-0.55	-1.78
GILEAD SCIENCES INC	0.2%	-0.20	0.88	0.2%	0.2%	1.57	0.71	-0.70	-0.40	-0.07	0.68	-1.17	0.32

**E X H I B I T 4** (continued) A Step-by-Step Example of Integrating Factors in a Discretionary Portfolio health care sectors, whereas it had no exposure to the industrials, utilities, or real estate sectors. A quick glance at the list of holdings reveals that the fund held well-known, large-cap stocks. From the second column, we also see that holding weights ranged between 5.7% and 0.2%.

Column 3 shows the exposure of the holdings to factor alpha, which in this example is the average exposure to the eight factors, normalized across the underlying global stock universe. For example, the largest holding, Verizon Communications, had positive exposure to size, yield, and value and negative exposure to growth, which corresponds to a relatively cheap, high-yielding, large-cap stock with below-average growth prospects. Overall, the fund has an exposure of 0.48 to the alpha signal, which shows that it had already taken advantage of tilting toward historically rewarded factors.

The hypothetical factor-tilted portfolio is constructed in a two-step process using Equation 2. In the first step, the original holding weights are multiplied by the appropriate multiplier; in the second step, the weights are rescaled to sum to 1. The holding-level multipliers are listed in column 4 and are calculated as follows (cf. Equation 2):

$$multiplier_i = 1 + c * \alpha_i \tag{8}$$

where the scaling coefficient c is set so that the active exposure of the tilted fund relative to the original reaches the target level of 0.2. The multipliers were bounded from above and below by 2 and 0.5. These limitations were imposed to limit turnover due to the tilting process and improve the investability of the resulting fund. The final multipliers are shown in column 4.

Next, in column 5, the original weights are multiplied by the multiplier, and finally, in column 6, the multiplied weights are rescaled to sum to 1. As a result of this process, the exposure of the fund to the alpha signal increased by 0.16. It slightly falls short of the target active exposure of 0.2 because of the investability limitations imposed on the stock-level multipliers. The result of this process was that we tended to overweight stocks with alpha signal exposure above the average exposure of the fund and tended to underweight stock with lower factor exposures.

In this section, we presented the details of the reweighting process for one fund at one particular date. In our backtests, we repeated the process for all funds to arrive at the statistics in Exhibit 3.

#### CONCLUSION

Asset owners use indexes as policy benchmarks and reference portfolios in their asset allocation. Index investors track cap-weighted indexes that seek to capture the market return. Active investors select securities and build portfolios that aim to outperform the market. All these types of investors may be able to benefit from incorporating factors into their process. More importantly, they may also be able to integrate factors without compromising other fundamentally important aspects of their strategies.

Asset owners require reference benchmarks to provide broad market coverage and diversification. They also require these benchmarks to have high investment capacity so that funds that track such benchmarks can absorb large allocations. Our analysis showed that using the Black–Litterman framework to integrate factor views into benchmark indexes in the examples discussed earlier did not reduce their market coverage or diversification characteristics. In fact, we observed that factor-tilted benchmarks became less concentrated because tilts generally effected a modest reallocation away from large-cap securities and into mid- and small-cap constituents.

Index fund managers require reference benchmarks to be liquid, investable, and tradable to enable them to manage large index-tracking portfolios efficiently and with relatively low implementation cost. Our results showed that factor-tilted market indexes in the examples discussed experienced improved performance historically while remaining highly liquid and investable. The tilt method in particular that anchors the modified index weights to the original market-cap weights had turnover and days-to-trade characteristics that were in line with those of the parent cap-weighted indexes.

Discretionary managers use fundamental analysis to select stocks and construct portfolios that seek to outperform the market. Many believe that their unique investment process and expert judgment enables them to generate alpha through judicious security selection. However, many discretionary managers operate in an increasingly difficult business and market environment. From a business perspective, they are often under pressure to reduce costs and improve performance. The market environment has also been challenging because quantitative easing increased correlations and a few large technology stocks dominated the market, which may have contributed to the difficulty in generating alpha from stock selection.

Our analysis confirmed that adding factors to active portfolios in the examples discussed led to substantial performance uplift historically. Crucially, the portfolio characteristics and the managers' stock selection contribution remained largely unchanged following the introduction of factor tilts. The portfolios held exactly the same securities; no names were added or removed. In addition, modified portfolio weights were highly correlated with the original weights that were established by the discretionary managers. In summary, our process of integrating factors in active portfolios in the examples discussed improved performance historically without altering the characteristics of these portfolios and without compromising the managers' ability to deploy their skills and generate alpha from stock selection.

### A P P E N D I X

#### SELECTION BIAS UNDER MULTIPLE TESTING

Financial researchers and practitioners have long ignored the effects of multiple testing on the significance of their results. In a world where analyzing vast amounts of data has become much cheaper, conducting multiple backtests with significantly different specifications on a strategy, alpha signal or a regression model has become a daily routine. However, with the profusion of backtests, the likelihood of a false discovery also increases significantly. To illustrate the seriousness of this problem, Fabozzi and Prado (2018) argue that the expected value of the best Sharpe ratio coming out of 100 independent backtests on a random walk would be around 2.5, despite the fact that clearly no alpha exists in this case. To avoid these types of errors, the usual significance statistics have to be adjusted for the fact that the final results are selected from a potentially large number of independent tests. This is what we set out to do in this appendix following the procedure described in Fabozzi and Prado (2018).

Although the factors used in this paper were taken from MSCI's Global Total Market Equity Model, and so not all of them were initially selected for their excess performance virtues, for the purpose of this statistical analysis, we treat all of them as potential alpha signals. The adjustment carried out below is thus approximate, and should only be taken as an illustration of the process.

The methodology described in Fabozzi and Prado (2018) prescribes three steps to address the problem of selection bias under multiple testing. First, we need to define the family of trials, that is, the collection of all results among which we selected the published result. In our case, during the building of the model, descriptors were aggregated into factors by simple linear combinations, and all individual and aggregated descriptors were tested separately. This brings the size of the trials to 52 (41 descriptors and 11 style factors with multiple descriptors).

Next, we need to define the number of significantly different experiments conducted, or the family size. In the case of strategy backtests, this is equivalent to the number of clusters such that the intra-cluster correlation is significantly higher than the inter-cluster correlation. In the GEMLT model, descriptors entering the definition of a factor were

#### Ехнівіт А1

Sharpe Ratio Cutoffs at the 5% Significance Level for Various Sample Sizes and Family Sizes, Assuming Normality of Returns

				# of	Families					
Annualized Sharpe Ratio	1	2	5	10	25	50	100	250	500	1000
12	1.83	2.25	2.79	3.21	3.79	4.27	4.80	5.61	6.34	7.24
24	1.22	1.47	1.78	2.00	2.29	2.50	2.71	2.99	3.20	3.42
36	0.98	1.18	1.41	1.58	1.79	1.94	2.09	2.28	2.43	2.57
48	0.84	1.01	1.21	1.35	1.52	1.64	1.76	1.92	2.03	2.14
60	0.75	0.90	1.07	1.19	1.34	1.45	1.55	1.69	1.78	1.88
120	0.53	0.63	0.74	0.83	0.93	1.00	1.07	1.15	1.21	1.27
180	0.43	0.51	0.60	0.67	0.75	0.81	0.86	0.93	0.98	1.03
240	0.37	0.44	0.52	0.58	0.65	0.70	0.74	0.80	0.84	0.88
300	0.33	0.39	0.47	0.52	0.58	0.62	0.66	0.72	0.75	0.79

significantly more correlated among themselves than with other factors or descriptors. So this brings the family size to 16 (16 style factors).

Finally, depending on the significance level, the number of observations, and the family size, the adjusted cut-offs for factor return Sharpe ratios can be calculated. For the derivation, we refer again to Fabozzi and Prado (2018). In the below table we plotted the annualized Sharpe ratio cutoffs, at the 5% significance level for various sample sizes and family sizes. We assumed returns were measured at a monthly frequency, since this was the rebalancing frequency for the factor portfolios presented in the paper. We also assumed normal return distribution, but note that adjustments for skewness and kurtosis are possible, and generally would lead to higher thresholds.

Following this analysis, we find that the Sharpe ratio cutoff relevant for the backtests presented in this paper, assuming 5% significance level, 279 monthly observations and 16 test families is 0.57.

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#### ADDITIONAL READING

#### Being Honest in Backtest Reporting: A Template for Disclosing Multiple Tests

FRANK J. FABOZZI AND MARCOS LÓPEZ DE PRADO The Journal of Portfolio Management https://jpm.pm-research.com/content/45/1/141

**ABSTRACT:** Selection bias under multiple testing is a serious problem. From a practitioner's perspective, failure to disclose the impact of multiple tests of a proposed investment strategy to clients and senior management can lead to the adoption of a false discovery. Clients will lose money, senior management will misallocate resources, and the firm may be exposed to reputational, legal, and regulatory risks. From the perspective of academic journals that publish evidence supporting an investment strategy, the failure to address selection bias under multiple testing threatens to invalidate large portions of the literature in empirical finance. In this article, the authors propose a template that practitioners should use to fairly disclose multiple tests involved in an alleged discovery when pitching strategies to clients and senior management. The same template could be used by contributors to academic journals so that referees, and ultimately readers, can assess the strategy. By disclosing this information, those who are charged with making the final decision about a discovery can evaluate the probability that the purported discovery is false.

### The Black-Litterman Model for Structured Equity Portfolios

ROBERT C JONES, TERENCE LIM, AND PETER J ZANGARI The Journal of Portfolio Management

https://jpm.pm-research.com/content/33/2/24

**ABSTRACT:** The Black-Litterman model enables the development of sound inputs for portfolio optimization. Before Black-Litterman, investors were often frustrated by the seemingly unreasonable solutions that portfolio optimization techniques would produce. Many either abandoned the technology or relinquished most of its benefits by applying so many constraints that the solution was largely predetermined. In fact, any "unreasonable" solutions have been not so much a problem with optimization per se, but rather the result of feeding inconsistent risk and return forecasts into an optimizer. To be effective in optimization, risk and return forecasts must be consistent with one another. When structured equity portfolio managers who develop views based on factors (like value or momentum) want to use the Black-Litterman model to construct equity portfolios, they generally focus on returns relative to a benchmark. The basic Black-Litterman approach is robust in this case and easily adaptable to the problem at hand.

### Efficient Replication of Factor Returns: Theory and Applications

Dimitris Melas, Raghu Suryanarayanan, and Stefano Cavaglia

The Journal of Portfolio Management https://jpm.pm-research.com/content/36/2/39

**ABSTRACT:** This article presents alternative methods for constructing factor-replicating portfolios, which include portfolios that have unit exposure to a target factor, zero exposure to other factors, and minimum portfolio risk. The authors provide empirical evidence that constrained factor portfolios, with a limited number of assets and relatively low turnover, tracked several Barra equity risk model pure factor returns reasonably well. They also illustrate how factor-mimicking portfolios could have been utilized in the past to enhance both passive and active investment strategies. Factor-mimicking portfolios can be used to hedge out the unintended factor exposures of conventional benchmarks, which are aimed at targeting a particular beta factor, and thus enable plan sponsors to better manage their optimal allocations to beta factor risks. Additionally, factor-mimicking portfolios can be utilized to hedge out the style exposures of active stock-picking strategies enabling active managers to capture pure alpha.